

(DN) Draw line m and construct lines p and q so that they are both perpendicular to line m .

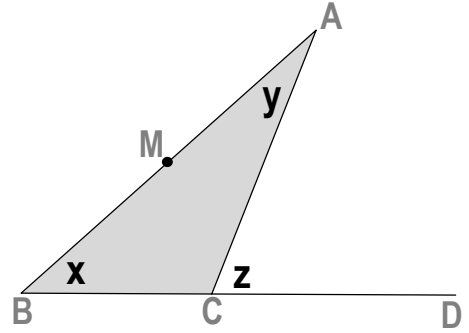
Name _____ Per _____

LO: I can use angle relationships to prove statements.

IMPRESS ME: How can you use your compass with your construction to make a square? Explain or execute.

(1) **Angles: Exterior angle theorem:** Proof by constructing a parallel line.

transparencies, dry erase markers, erasers, compass



(a) The **exterior angle theorem** states that (see N12)

$z = \underline{\hspace{1cm}} + \underline{\hspace{1cm}}$

(b) Rotate $\angle ABC$ 180° around the midpoint of \overline{AB} .

(c) I know that $m\angle ABC = x$ because it is **given** in the diagram.

Therefore, I know that $m\angle A'B'C' = \underline{\hspace{1cm}}$ because _____

(d) I know that $m\angle C'AC = \underline{\hspace{1cm}} + \underline{\hspace{1cm}}$ because _____

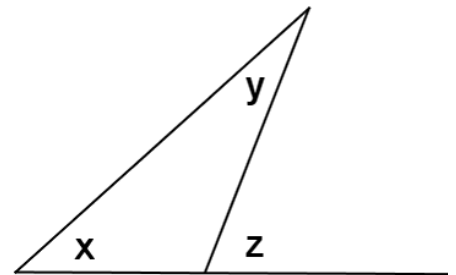
(e) I know that $\overline{C'A}$ is _____ to \overline{BC} because _____

(f) I know that $m\angle C'AC = m\angle ACD$ because _____

(g) I know that $x + y = z$ because _____

(2) **Angles: Exterior angle theorem:** Proof by angle relationship & algebra

transparencies, dry erase markers, erasers



(a) Add a w to the empty angle in the diagram

(b) I know that $x + y + w = 180$ because _____

(c) I know that $z + w = 180$ because _____

(d) I know that $x + y + w = z + w$ because _____

(e) I know that $x + y = z$ because _____

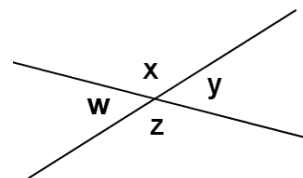
(3)
transparencies, dry
erase markers,
erasers

Angles: Proving relationships

When writing proofs, you can rely on **facts** that you know – facts about **angle relationships, transformations, parallel lines**. You can add **auxiliary lines** or **letters** to angles or points of intersection. You can construct to help you see relationships you might use in a proof. As you work through each proof in this lesson, refer to the notes pages N11 and N12. Prove each statement below. (you may not need all of the lines provided for you) Do 6 of the 10 problems

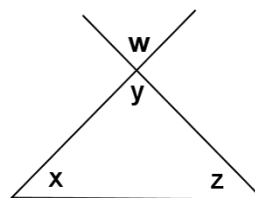
(a) PROVE: *Vertical angles are equal.* (suggestion: 2 linear pairs, substitution, and inverse operations)

- (1) I know that _____ and _____ are vertical angles
because _____
- (2) I know that _____
because _____
- (3) I know that _____
because _____
- (4) I know that _____
because _____
- (5) I know that _____
because _____

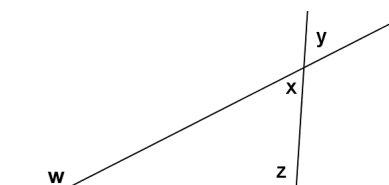


(b) PROVE: $w + x + z = 180^\circ$ (suggestions: vertical angles, triangle sum, substitution)

- (1) I know that _____
because _____
- (2) I know that _____
because _____
- (3) I know that _____
because _____



(c) PROVE: $w = y + z$ (suggestions: vertical angles, exterior angle theorem, substitution)

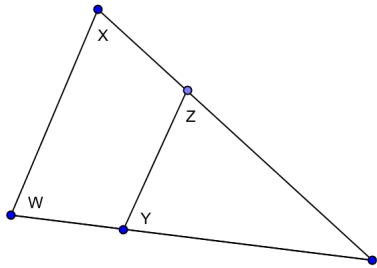


I know that . . .	because . . .

(3) **Angles: Rotations and proving the**

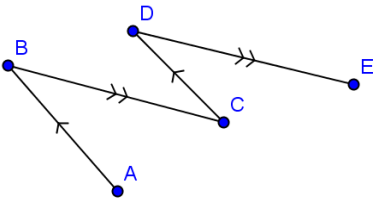
cont.

(d) PROVE: $y + z = w + x$ (suggestions: add a letter, triangle sum, substitution)



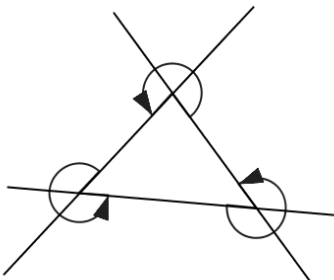
I know that . . .	because . . .

(e) PROVE: $\angle ABC \cong \angle CDE$ (suggestions: note the pairs of parallel lines)



I know that . . .	because . . .

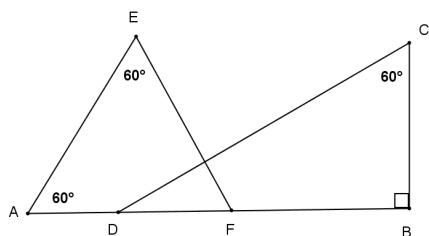
(f) PROVE: *the sum of the marked angles is 900°* (suggestions: add labels, triangle 180° , angles at a point)



I know that . . .	because . . .

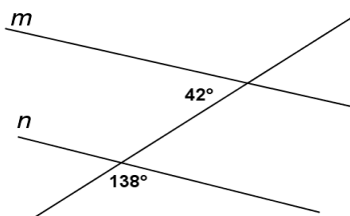
(3) **Angles: Rotations and proving the**

cont.

 (g) PROVE: $\overline{DC} \perp \overline{EF}$ (suggestions: \perp means perpendicular means 90° , add letters, triangle 180°)


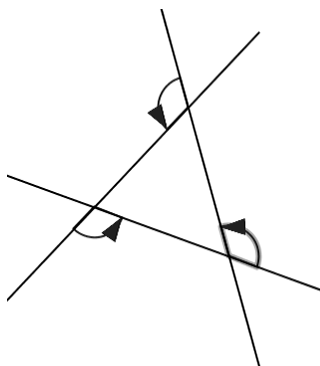
I know that ...

because ...

 (h) PROVE: $m \parallel n$ (suggestions: add letters, corresp., linear pair, alt. int., vert., alt. ext., same side ext.)


I know that ...

because ...

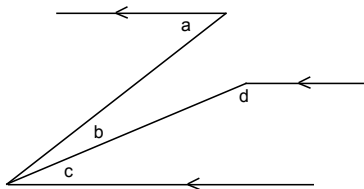
 (i) PROVE: *the sum of the marked angles is 360°* (suggestions: add letters, linear pair, triangle sum)


I know that ...

because ...

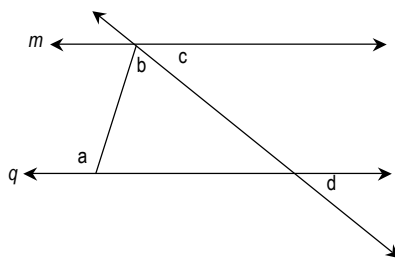
(3) **Angles: Rotations and proving the**

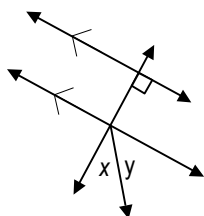
cont.

 (j) PROVE: $a + d - b = 180^\circ$ (suggestions: alt. int., same side int.)


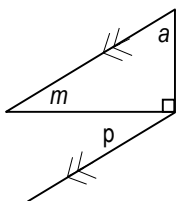
I know that ...	because ...

 (4) **Exit Ticket**

 Given that $q \parallel m$, prove $a = b + d$.

 (5) **Homework** You may need to add letters to the diagrams to complete your proof.

 (1) PROVE: $x + y = 90^\circ$


I know that ...	because ...

 (2) PROVE: $a + p = 90^\circ$


I know that ...	because ...

